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***The Maximum Norm Analysis of a Nonmatching Grids
Method for Nonlinear Parabolic PDES with bilaplacian
operator***

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